

$$\psi_0(x) = e^{-i v x} e^{-(x-L)^2/\sigma^2}$$